



Supplement of

Decadal variability and trends in extratropical Rossby wave packet amplitude, phase, and phase speed

Georgios Fragkoulidis

Correspondence to: Georgios Fragkoulidis (gfragkou@uni-mainz.de)

The copyright of individual parts of the supplement might differ from the article licence.

Contents

1	Annual time series of RWP amplitude over N America, Europe, C Asia, and NW Pacific	2	
2	Annual time series of RWP amplitude over NE Pacific and N Atlantic: Comparison between CERA-20C members	3	
3	Annual time series of RWP phase speed over NE Pacific and N Atlantic	3	
4	Decadal trends in 300 hPa zonal wind	4	
5	Decadal trends in high- E extremes	4	
6	Decadal trends in low- c_p extremes	5	
7	Decadal trends in compound extremes	5	
8	Temporal variation of trends in RWP extremes	6	
9	Reanalysis data retrieval	8	
10	Computation methods	8	
Bi	Bibliography		





Fig. S1: (a) LOWESS time series of DJF-mean *E* at 300 hPa over N America (Fig. 2) based on the CERA-20C (red), ERA-20C (purple), JRA-55 (yellow), MERRA-2 (blue), and ERA5 (black) reanalysis. The thin red and black lines correspond to the original DJF-mean time series in CERA-20C and ERA5, respectively. (b) Same as (a), but for the Europe region. (c,d) Same as (a,b), but for the JJA season.



Fig. S2: Same as Fig. S1, but for the C Asia (a,c) and NW Pacific (b,d) regions.

2 Annual time series of RWP amplitude over NE Pacific and N Atlantic: Comparison between CERA-20C members



Fig. S3: (a) LOWESS time series of DJF-mean E at 300 hPa over NE Pacific (Fig. 2) based on two CERA-20C members (member #1 corresponds to the one used in Fig. 3 of the paper). The thin lines correspond to the original DJF-mean time series. (b) Same as (a), but for the N Atlantic region. (c,d) Same as (a,b), but for the JJA season.

3 Annual time series of RWP phase speed over NE Pacific and N Atlantic



Fig. S4: (a) LOWESS time series of DJF-mean c_p at 300 hPa over NE Pacific (Fig. 2) based on CERA-20C (red), ERA-20C (purple), JRA-55 (yellow), MERRA-2 (blue), and ERA5 (black). The thin red and black lines correspond to the original DJF-mean time series in CERA-20C and ERA5, respectively. (b) Same as (a), but for the N Atlantic region. (c,d) Same as (a,b), but for the JJA season.

4 Decadal trends in 300 hPa zonal wind



Fig. S5: Maps of 1979–2019 linear trends (Theil-Sen estimator; colour shading) in the standardized seasonalmean zonal wind (u) at 300 hPa for (a) DJF, (b) MAM, (c) JJA, and (d) SON in ERA5. Red hatching indicates areas where the monotonicity of the trend is statistically significant at the 0.10 significance level. Black contours correspond to the multi-year mean u values of the respective season.

5 Decadal trends in high-*E* extremes



Fig. S6: Maps of 1979–2019 linear trends (Theil-Sen estimator; colour shading) in the number of high-E extremes at 300 hPa for (a) DJF, (b) MAM, (c) JJA, and (d) SON in ERA5. Red hatching indicates areas where the monotonicity of the trend is statistically significant at the 0.10 significance level.

6 Decadal trends in low- c_p extremes



Fig. S7: Same as Fig. S6, but for low- c_p extremes at 300 hPa.

7 Decadal trends in compound extremes

Fig. S8: Same as Fig. S6, but for compound extremes at 300 hPa.

8 Temporal variation of trends in RWP extremes

Fig. S9: Maps of 1979–1999 linear trends (Theil-Sen estimator; colour shading) in the number of MAM (a) high-E extremes, (c) low- c_p extremes, and (e) compound high-E/low- c_p extremes at 300 hPa in ERA5. (b),(d),(f) Same as (a),(c),(e), but for 1999–2019. Red hatching indicates areas where the monotonicity of the trend is statistically significant at the 0.10 significance level.

Fig. S10: Same as Fig. S9, but for JJA.

Fig. S11: Same as Fig. S9, but for SON.

9 Reanalysis data retrieval

The reanalysis datasets used in this study are described and referenced in section 2.1 of the paper. They have been freely retrieved from the online sources listed in Table S1.

	Dataset	Citation & Online Source	Web Address
1	ERA5/ERA5.1	Hersbach et al. (2018). Source:	https://doi.org/10.24381/cds.
		Copernicus Climate Change Service	bd0915c6, https://confluence.
		(C3S) Climate Data Store (CDS).	<pre>ecmwf.int/pages/viewpage.</pre>
			action?pageId=181130838
2	MERRA-2	NASA Global Modeling and Assimila-	https://disc.gsfc.nasa.gov/
		tion Office (GMAO) (2015). Source:	datasets/M2I6NPANA_5.12.4/
		Goddard Earth Sciences Data and	summary
		Information Services Center (GES	
		DISC).	
3	JRA-55	Japan Meteorological Agency, Japan	https://rda.ucar.edu/datasets/
		(2013). Source: Research Data	ds628.0/
		Archive at NCAR/CISL.	
4	ERA-20C	ECMWF Public Datasets	https://apps.ecmwf.int/
			datasets/data/era20c-daily/
			levtype=sfc/type=an/
5	CERA-20C	ECMWF Public Datasets	https://apps.ecmwf.int/
			datasets/data/cera20c/levtype=
			sfc/type=an/

Table S1: List of reanalysis datasets used in this study and their online sources.

10 Computation methods

The computations in this study were conducted in Python 3.9.7. The Climate Data Operators (CDO) 1.9.8 (Schulzweida 2021) was used for basic handling of the reanalysis data files. In terms of Python libraries, netCDF4 1.5.4 (Unidata 2018) was used for reading the data, Matplotlib 3.3.3 (Hunter 2007) was used for plotting, while NumPy 1.22.0 (Harris et al. 2020) and SciPy 1.5.3 (Virtanen et al. 2020) were used for routine array operations and data analysis. Finally, Table S2 lists the main Python modules/functions that were used in this study.

	Module (version)	Notes	More info
1	scipy.fft $(1.5.3)$	1-D discrete Fourier Transform	https://docs.scipy.org/
		(Fast Fourier transform algorithm)	
2	<pre>scipy.stats.gaussian_</pre>	1-D and 2-D kernel-density es-	https://docs.scipy.org/
	kde $(1.5.3)$	timate using Gaussian kernels	
		(Figs. 4,9)	
3	pyMannKendall $(1.4.1)$	Mann-Kendall trend test and Theil-	https://github.com/
		Sen estimator (Hussain and Mah-	mmhs013/pymannkendall
		mud 2019)	

Table S2: List of Python modules used in this study. In the Notes column we indicate their specific applicationin the paper.

Bibliography

- Harris, C. R., Millman, K. J., van der Walt, S. J., Gommers, R., Virtanen, P., Cournapeau, D., Wieser, E., Taylor, J., Berg, S., Smith, N. J., Kern, R., Picus, M., Hoyer, S., van Kerkwijk, M. H., Brett, M., Haldane, A., del Río, J. F., Wiebe, M., Peterson, P., Gérard-Marchant, P., Sheppard, K., Reddy, T., Weckesser, W., Abbasi, H., Gohlke, C., and Oliphant, T. E.: Array programming with NumPy, Nature, 585, 357–362, https://doi.org/10.1038/s41586-020-2649-2, 2020.
- Hersbach, H., Bell, B., Berrisford, P., Biavati, G., Horányi, A., Muñoz Sabater, J., Nicolas, J., Peubey, C., Radu, R., Rozum, I., Schepers, D., Simmons, A., Soci, C., Dee, D., and Thépaut, J.-N.: ERA5 hourly data on pressure levels from 1979 to present (Accessed on 01-11-2020), https://doi.org/ 10.24381/cds.bd0915c6, 2018.
- Hunter, J. D.: Matplotlib: A 2D graphics environment, Computing in Science and Engineering, 9, 90–95, https://doi.org/10.1109/MCSE.2007.55, 2007.
- Hussain, M. and Mahmud, I.: pyMannKendall: a python package for non parametric Mann Kendall family of trend tests., Journal of Open Source Software, 4, 1556, https://doi.org/10.21105/joss. 01556, 2019.
- Japan Meteorological Agency, Japan: JRA-55: Japanese 55-year Reanalysis, Daily 3-Hourly and 6-Hourly Data (Accessed on 01-08-2020), URL https://doi.org/10.5065/D6HH6H41, 2013.
- NASA Global Modeling and Assimilation Office (GMAO): MERRA-2 inst6_3d_ana_Np: 3d, 6-Hourly, Instantaneous, Pressure-Level, Analysis, Analyzed Meteorological Fields V5.12.4 (Accessed on 07-06-2020), https://doi.org/10.5067/A7S6XP56VZWS, 2015.
- Schulzweida, U.: CDO User Guide, https://doi.org/10.5281/zenodo.5614769, 2021.
- Unidata: Network Common Data Form (NetCDF) [software], https://doi.org/10.5065/D6H70CW6, 2018.
- Virtanen, P., Gommers, R., Oliphant, T. E., Haberland, M., Reddy, T., Cournapeau, D., Burovski, E., Peterson, P., Weckesser, W., Bright, J., van der Walt, S. J., Brett, M., Wilson, J., Millman, K. J., Mayorov, N., Nelson, A. R. J., Jones, E., Kern, R., Larson, E., Carey, C. J., Polat, İ., Feng, Y., Moore, E. W., VanderPlas, J., Laxalde, D., Perktold, J., Cimrman, R., Henriksen, I., Quintero, E. A., Harris, C. R., Archibald, A. M., Ribeiro, A. H., Pedregosa, F., van Mulbregt, P., and SciPy 1.0 Contributors: SciPy 1.0: Fundamental Algorithms for Scientific Computing in Python, Nature Methods, 17, 261–272, https://doi.org/10.1038/s41592-019-0686-2, 2020.