Supplement of Weather Clim. Dynam., 6, 1661–1681, 2025 https://doi.org/10.5194/wcd-6-1661-2025-supplement © Author(s) 2025. CC BY 4.0 License.





Supplement of

Signal, noise and skill in sub-seasonal forecasts: the role of teleconnections

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Signal, noise and skill in sub-seasonal forecasts: the role of teleconnections

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Supplementary Materials

Table S1: Spatial correlation coefficients (30°N-90°N) between the forecast skill (ρ) and the forecast properties (σ_{EM}^2 , σ_{ES}^2 , STN, ρ_{perf}^{STN} , ρ_{perf}^{ACC}) for T2M in CTRL. The values above the diagonal are for Weeks 3-4. The values below the diagonal are for Weeks 5-6.

| | ρ | $ ho_{perf}^{STN}$ | $ ho_{perf}^{ACC}$ | STN | σ_{EM}^2 | $\sigma_{\!\scriptscriptstyle ES}^2$ |
|--------------------------------------|-------|--------------------|--------------------|-------|-----------------|--------------------------------------|
| ρ | 1 | 0.77 | 0.77 | 0.75 | -0.23 | -0.39 |
| $ ho_{perf}^{STN}$ | 0.70 | 1 | 1 | 0.97 | -0.21 | -0.46 |
| $ ho_{perf}^{ACC}$ | 0.69 | 1 | 1 | 0.96 | -0.21 | -0.46 |
| STN | 0.69 | 0.97 | 0.96 | 1 | -0.21 | -0.43 |
| σ_{EM}^2 | -0.28 | -0.30 | -0.30 | -0.28 | 1 | 0.91 |
| $\sigma_{\!\scriptscriptstyle ES}^2$ | -0.45 | -0.54 | -0.55 | -0.48 | 0.90 | 1 |

Table S2: Spatial correlation coefficients (30°N-90°N) between the changes in the forecast skill ($\Delta \rho$) and changes in the forecast properties ($\Delta \sigma_{EM}^2$, $\Delta \sigma_{ES}^2$, ΔSTN , $\Delta \rho_{perf}^{STN}$, $\Delta \rho_{perf}^{ACC}$) for T2M in the relaxation experiments.

| | TROP | | | | | STRAT | | | | |
|-----------|------------------------|-----------------------|--------------|--------------------------|--------------------------|------------------------|-----------------------|--------------|--------------------------|---------------------------|
| | $\Delta \sigma_{EM}^2$ | $\Delta\sigma_{ES}^2$ | ΔSTN | Δho_{perf}^{STN} | Δho_{perf}^{ACC} | $\Delta \sigma_{EM}^2$ | $\Delta\sigma_{ES}^2$ | ΔSTN | Δho_{perf}^{STN} | Δho_{perf}^{ACC} |
| Weeks 1-2 | -0.03 | -0.05 | 0.25 | 0.42 | 0.41 | 0.04 | -0.09 | -0.03 | 0.01 | 0.02 |
| Weeks 3-4 | 0.10 | -0.06 | 0.44 | 0.51 | 0.50 | 0.29 | -0.15 | 0.16 | 0.28 | 0.28 |
| Weeks 5-6 | 0.03 | -0.23 | 0.34 | 0.36 | 0.34 | 0.14 | 0.00 | 0.08 | 0.16 | 0.16 |

Table S3: Spatial correlation coefficients (30°N-90°N) between the forecast skill (ρ) and the forecast properties (σ_{EM}^2 , σ_{ES}^2 , STN, ρ_{perf}^{STN} , ρ_{perf}^{ACC}) for TP in CTRL. The values above the diagonal are for Weeks 3-4. The values below the diagonal are for Weeks 5-6.

| | ρ | $ ho_{perf}^{STN}$ | $ ho_{perf}^{ACC}$ | STN | σ_{EM}^2 | σ_{ES}^2 |
|--------------------|------|--------------------|--------------------|------|-----------------|-----------------|
| ρ | 1 | 0.42 | 0.41 | 0.42 | 0.23 | 0.16 |
| $ ho_{perf}^{STN}$ | 0.43 | 1 | 1 | 0.99 | 0.43 | 0.30 |
| $ ho_{perf}^{ACC}$ | 0.42 | 1 | 1 | 0.98 | 0.43 | 0.30 |
| STN | 0.42 | 0.99 | 0.98 | 1 | 0.43 | 0.30 |
| σ_{EM}^2 | 0.22 | 0.46 | 0.46 | 0.45 | 1 | 0.96 |
| σ_{ES}^2 | 0.14 | 0.30 | 0.30 | 0.28 | 0.96 | 1 |

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Table S4: Spatial correlation coefficients between the changes in the forecast skill ($\Delta \rho$) and changes in the forecast properties ($\Delta \sigma_{EM}^2$, $\Delta \sigma_{ES}^2$, ΔSTN , $\Delta \rho_{perf}^{STN}$, $\Delta \rho_{perf}^{ACC}$) for TP in the relaxation experiments.

| | TROP | | | | STRAT | | | | | |
|-----------|------------------------|------------------------|--------------|---------------------------|---------------------------|------------------------|-----------------------|--------------|---------------------------|---------------------------|
| | $\Delta \sigma_{EM}^2$ | $\Delta \sigma_{ES}^2$ | ΔSTN | Δho_{perf}^{STN} | Δho_{perf}^{ACC} | $\Delta \sigma_{EM}^2$ | $\Delta\sigma_{ES}^2$ | ΔSTN | Δho_{perf}^{STN} | Δho_{perf}^{ACC} |
| Weeks 1-2 | 0.06 | -0.12 | 0.15 | 0.13 | 0.13 | 0.01 | -0.03 | 0.02 | 0.04 | 0.04 |
| Weeks 3-4 | 0.26 | -0.26 | 0.33 | 0.34 | 0.33 | 0.02 | 0.02 | 0.07 | 0.07 | 0.07 |
| Weeks 5-6 | 0.33 | -0.22 | 0.39 | 0.41 | 0.40 | 0.08 | -0.08 | 0.14 | 0.15 | 0.15 |

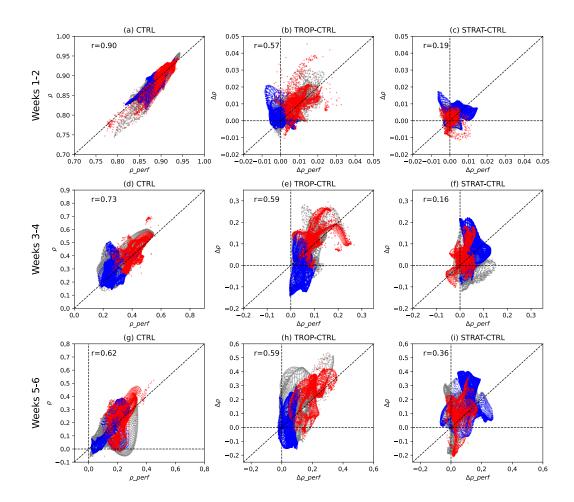


Figure S1: (a,d,g) Scatterplots between ρ and ρ_{perf}^{ACC} for SLP anomalies at each grid point between 30°N and 90°N in CTRL. 2nd and 3rd columns show differences for ρ and ρ_{perf}^{ACC} between relaxation experiments (TROP and STRAT respectively) and CTRL. Spatial correlation coefficients between ρ and ρ_{perf}^{ACC} fields are shown as r-values in each panel. Red dots mark grid points south of 40°N, blue dots mark grid points north of 60°N, and grey dots mark grid points between 40°N-60°N.

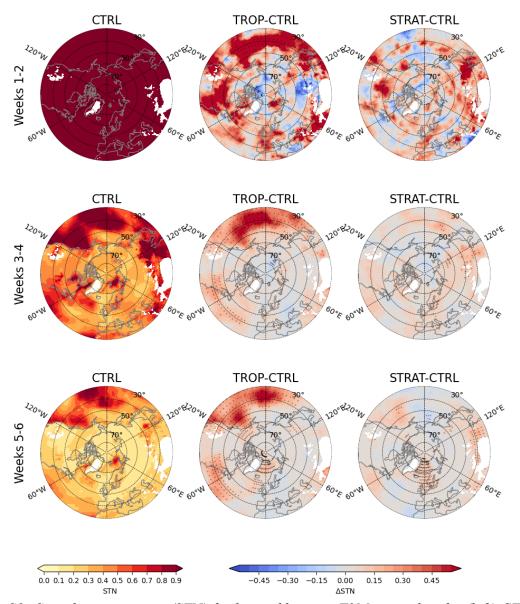


Figure S2: Signal to noise ratio (STN) for bi-weekly mean T2M anomalies for (left) CTRL; and the differences between ρ in (center) TROP and (right) STRAT experiments with respect to CTRL. Stippling in (center, right) indicates significant differences between CTRL and the respective relaxation experiments.

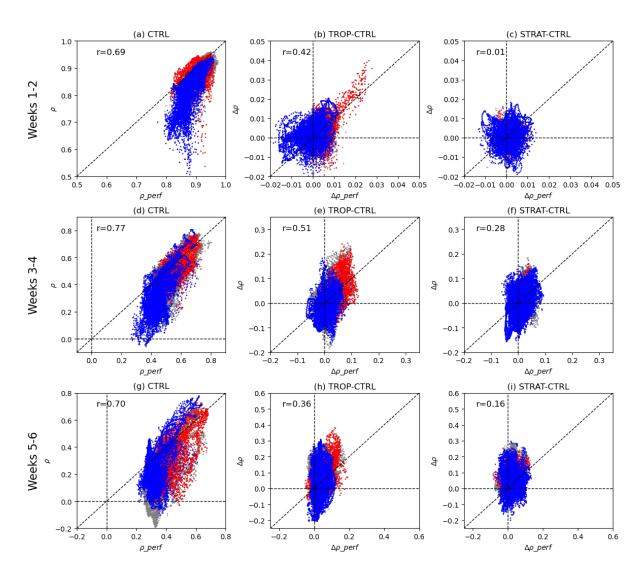


Figure S3: (a,d,g) Scatterplots between ρ and $\Delta \rho_{perf}^{STN}$ for T2M anomalies at each grid point between 30 °N and 90 °N in CTRL. 2nd and 3rd columns show differences for ρ and $\Delta \rho_{perf}^{STN}$ between relaxation experiments (TROP and STRAT respectively) and CTRL. r-values show spatial correlation coefficients between ρ and $\Delta \rho_{perf}^{STN}$ fields. Red dots mark grid points south of 40 °N, blue dots mark grid points north of 60 °N, and grey dots mark grid points between 40 °N-60 °N.

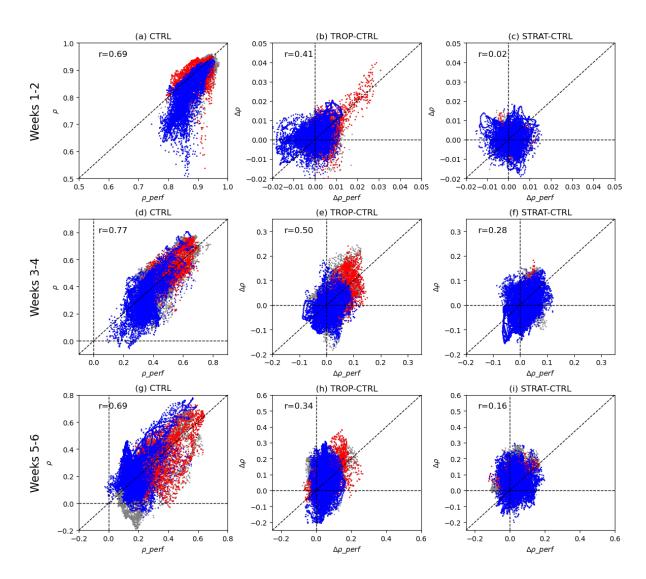


Figure S4: The same as Fig.S2 but for ρ_{perf}^{ACC} instead of ρ_{perf}^{STN} .

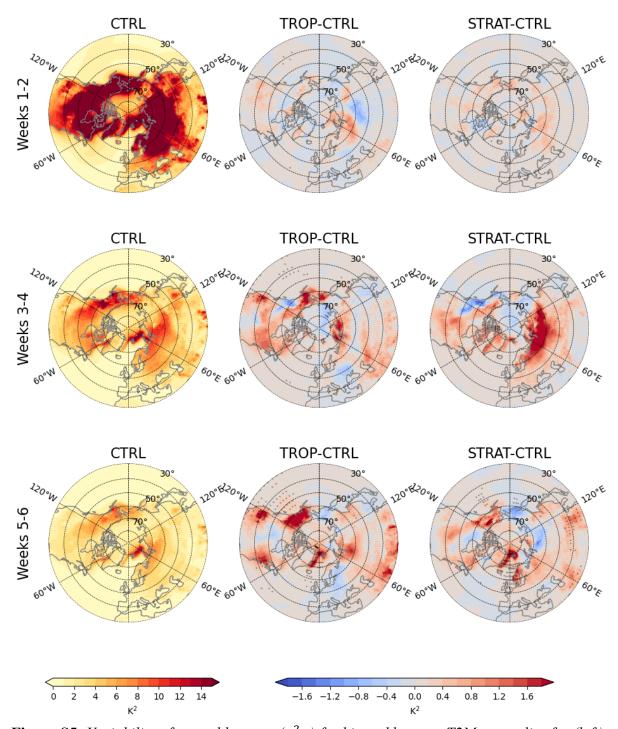


Figure S5: Variability of ensemble mean (σ_{EM}^2) for bi-weekly mean T2M anomalies for (left) CTRL; and the differences between σ_{EM}^2 in (center) TROP and (right) STRAT experiments with respect to CTRL. Stippling in (center, right) indicates significant differences between CTRL and the respective relaxation experiments.

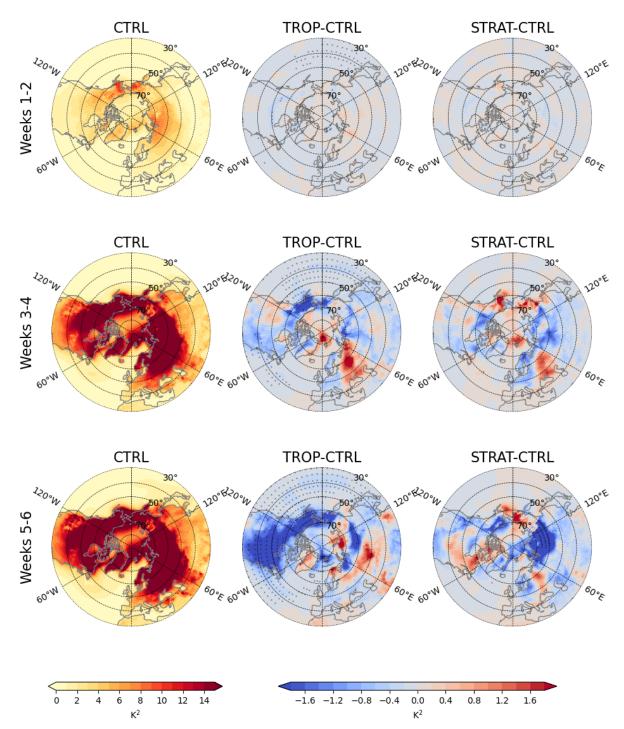


Figure S6: Ensemble spread (σ_{ES}^2) for bi-weekly mean T2M anomalies for (left) CTRL; and the differences between σ_{ES}^2 in (center) TROP and (right) STRAT experiments with respect to CTRL. Stippling in (center, right) indicates significant differences between CTRL and the respective relaxation experiments.

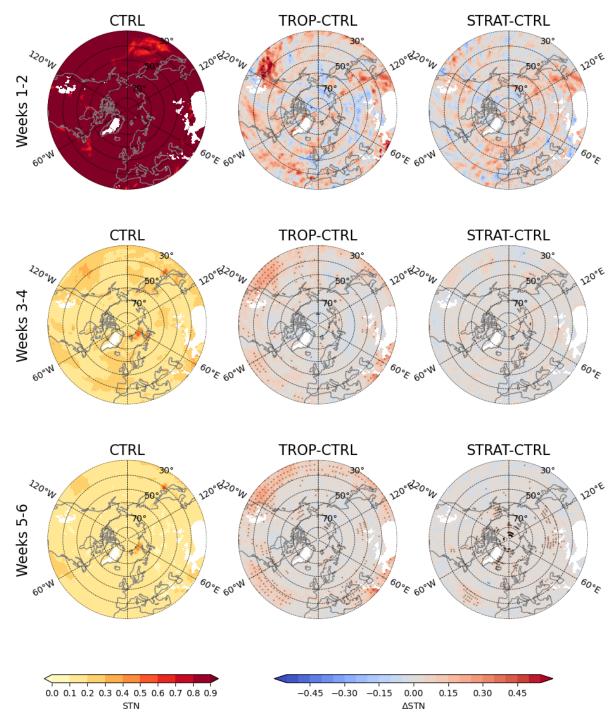


Figure S7: Signal to noise ratio (STN) for bi-weekly mean TP anomalies for (left) CTRL; and the differences between ρ in (center) TROP and (right) STRAT experiments with respect to CTRL. Stippling in (center, right) indicates significant differences between CTRL and the respective relaxation experiments.

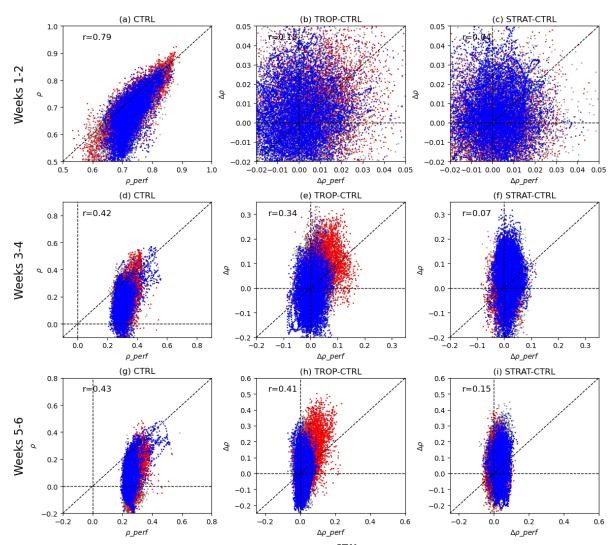


Figure S8: (a,d,g) Scatterplots between ρ and ρ_{perf}^{STN} for TP anomalies at each grid point between 30 N and 90 N in CTRL. 2nd and 3rd columns show differences for ρ and ρ_{perf}^{STN} between relaxation experiments (TROP and STRAT respectively) and CTRL. r-values show spatial correlation coefficients between ρ and ρ_{perf}^{STN} fields. Red dots mark grid points south of 40 N, blue dots mark grid points north of 60 N, and grey dots mark grid points between 40 N-60 N.

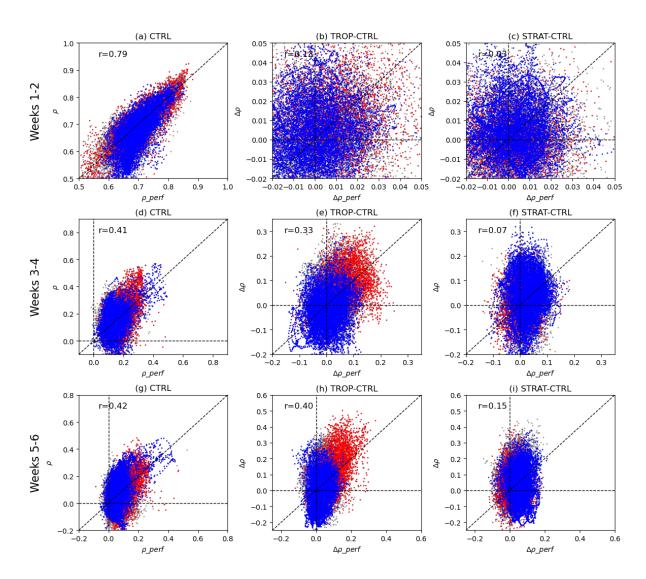


Figure S9: The same as Fig.S7 but for ρ_{perf}^{ACC} instead of ρ_{perf}^{STN} .

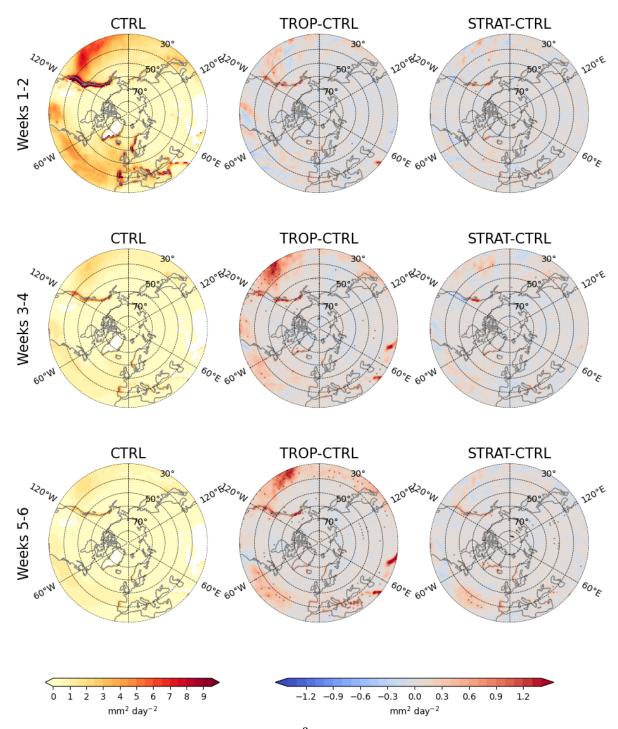


Figure S10: Variability of ensemble mean (σ_{EM}^2) for bi-weekly mean TP anomalies for (left) CTRL; and the differences between σ_{EM}^2 in (center) TROP and (right) STRAT experiments with respect to CTRL. Stippling in (center, right) indicates significant differences between CTRL and the respective relaxation experiments.

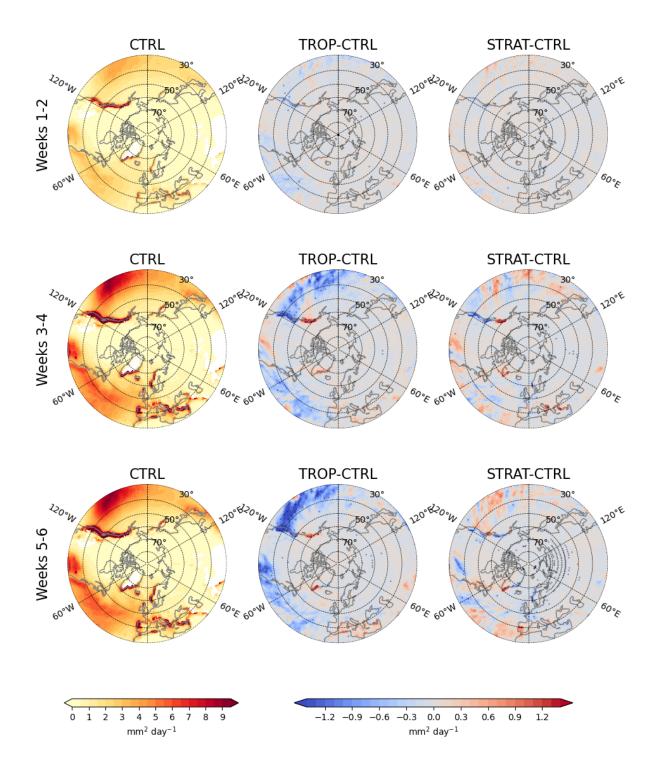


Figure S11: Ensemble spread (σ_{ES}^2) for bi-weekly mean TP anomalies for (left) CTRL; and the differences between σ_{ES}^2 in (center) TROP and (right) STRAT experiments with respect to CTRL. Stippling in (center, right) indicates significant differences between CTRL and the respective relaxation experiments.